

MTH 113 Test 2 (Chapter 5)

1. (14 pts.) Suppose that $\sin \alpha = \frac{4}{5}$ for a quadrant II angle α and $\sin \beta = \frac{5}{13}$ for a quadrant I angle β . Find the exact value of the following (hint: find sin / cos / tan of the angles first – simplify / leave in radical signs)...

$\sin (\alpha - \beta)$

$\cos (\alpha + \beta)$

2. (6 pts.) Find the exact value (include radical signs / leave no radical sign in the denominator as necessary) of $\tan(105^\circ) = \tan(45^\circ + 60^\circ)$ using the sum formula

3. (14 pts.) Suppose that $\sin \theta = \frac{7}{9}$ for a quadrant I angle θ . Find the exact value of the following (leave in radical signs / simplify)...

$\sin (2\theta)$

$\cos (2\theta)$

4. (8 pts.) Use a half-angle formula to find the exact value (leave in radical signs as necessary) of **$\tan(75^\circ)$**

--- hint: use one of the tan half-angle formulas without a radical sign ---

5. (10 pts.) Express each sum or difference as a product (if possible, find this product's exact value)

$\cos(5x) + \cos(3x)$

$\sin(165^\circ) - \sin(105^\circ)$

6. (10 pts.) Express each product as a sum or difference

$\sin(7x) \cos(3x)$

$\sin(5x) \sin(2x)$

7. (16 pts.) Solve each equation (find all solutions on the interval $[0, 2\pi)$ answer in radians)

$\cos 2x = \frac{1}{2}$

$\sin^2(\theta) - 5 = 4\sin(\theta)$

8. (7 pts.) With Easter approaching, the Easter Bunny is practicing his egg-throwing skills. If he wants to throw his eggs with an initial velocity of $v_0 = 90$ feet per second, at what angle of elevation will he need to throw it to intercept someone standing 100 feet away (round answer to 2 decimal places)? Use the formula...

$$d = \frac{v_0^2}{16} \sin \theta \cos \theta$$



BONUS: