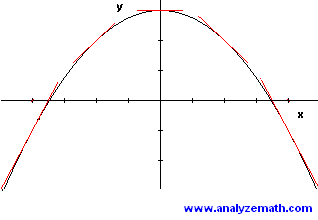
**Section 3.4** (Concavity and the Second Derivative Test)

Examine the slopes of the tangent lines in the following graph of a concave down function.

Is there a critical point? relative maximum / minimum?

Are the slopes increasing or decreasing?

If **f ``(x) > 0** for all x in a given interval (2nd derivative is positive, meaning that the slopes of the tangent lines are increasing), then f(x) is **concave up** on that interval.

If **f ``(x) < 0** for all x in a given interval (2nd derivative is negative, meaning that the slopes of the tangent lines are decreasing), then f(x) is **concave down** on that interval.

What if f ``(x) = 0?

Example: Determine open intervals on which the graph of f(x) = x3 – 3x2 + 1 is concave up or concave down.

Example: Determine open intervals on which the graph of f(x) = is concave up or concave down.

A point of inflection on the graph of f is a point (f ``(x) = 0) where concavity changes from down to up (or vice versa)

Example: Find the points of inflection and discuss concavity of f(x) = 2x4 – 8x + 3

Second derivative test when f `(c) = 0 and f ``(c) exists:

1. If f ``(c) > 0, then f has a relative minimum at (c,f(c))
2. If f ``(c) < 0, then f has a relative maximum at (c,f(c))

Example: Find all relative extrema of f(x) = x3 – 5x2 + 7x